## $\pi \mathrm{N}-\pi \mathrm{N}$ in J-PARC

## Proposal on measurements of the spin rotation parameters A and R

 at the J-PARC in the resonance region of the $\pi \mathrm{N}$-elastic scattering (The key experiment in the baryon spectroscopy)Petersburg Nuclear Physics Institute (Gatchina, Leningrad district)
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\piN-\piN in J-PARC
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## Abstract

Pion-nucleon interaction leading to the formation of nonstrange baryon resonances is one of fundamental interactions in the elementary particle physics. Nowadays there exists the evident disagreement between the number and characteristics of baryon resonances extracted from experimental data by different partial wave analysis (PWA) collaborations and those predicted by different theoretical models. The difference between PWA results is due amongst other things to the twofold ambiguities, which are inherent to the PWA procedure.

The spin rotation parameters A and R measurements in the pion-nucleon elastic scattering is practically the unique reliable method to exclude the twofold ambiguities from the $\pi \mathrm{N}$-amplitudes. In 2006 year the new PWA VPI-GWU (SP06) was published. Predictions of this analysis for the spin rotation parameters A and R are deducted by creation of given proposals.

## Introduction.

## 1. Introduction

The baryon resonances were discovered in 1950 year [Y.Fujimoto, H.Miyazawa; Progr. Theor. Phys. 5 (1950) 1052] in the reaction of the photoproduction. T.Nakano, K.Nishigima, M.Gell-Mann in 1953 year introduced the concepts of baryon number $\mathrm{N}_{\mathrm{b}}$ and strangeness S .

But before now (2006 year) the world scientific community have not a complete picture of the $\pi \mathrm{N}$ interactions. A uniquely determined $\pi \mathrm{N}$-amplitude is absent in the resonance region of the $\pi \mathrm{N}$-interactions. We don't know correctly - how many $\mathrm{N}^{*}, \Delta, \Lambda, \Sigma, \Xi, \Omega$ baryons there exist - neither experimentally, nor theoretically. There is no way in which it can be possible to resolve this problem except by a careful experimental study of the all $\pi \mathrm{N}$-interaction channels in total resonance region. If the high intensity pion beam with corresponding momentum will be realized at J-PARC, it will give the unique possibility to resolve this problem by means of every $\pi \mathrm{N}$ interaction channel experimental investigation.

Historically, the best information came from $\pi \mathrm{N}$ experiments, a situation that still holds now [1]. Pionnucleon interaction leading to the formation of nonstrange baryon resonances is one of fundamental interactions in the elementary particle physics. The interest in the study of baryon resonances has led to the important discovery of $\operatorname{SU}(3)$ symmetry. Just a multi-resonance structure of $\pi \mathrm{N}$-system has given a power impulse to developing quark-gluon models of baryons. Although many excited states of baryons were found, the quality and scope of the data limited the analyses [2].

> Physics goals.

## 2. Physics Goals

This experiment was aimed at next goals:
> (I) To obtain new experimental data for unambiguous reconstruction of $\pi p$-elastic amplitudes in the range of pion beam momentum and angles where the largest disagreement between predictions of the existing PWA's is observed;
> (II) To prove the choice of the transverse amplitude zero trajectory (solution branch);

The specific feature of measurements of the spin rotation parameters is that it is not necessary to make measurements in the full energy and angle ranges. It is enough to measure these parameters in some limited intervals of kinematical variables - that can be determined beforehand on the base of existing PWAs - in order to eliminate the problem of PWA ambiguities.

In Tables 3 and 4 we present these limited intervals of kinematical variables for the second resonance region of $\pi \mathrm{N}$-elastic scattering, which cover masses of baryon resonances from 1400 to 2000 MeV . The intervals were determined by analyzing zero trajectories of $\pi \mathrm{N}$ transverse amplitudes obtained for four existing global PWAs: KA84 $\left(\mathrm{T}_{\pi}=0.02-10 \mathrm{GeV}\right)$ [4], CMB $\left(\mathrm{T}_{\pi}=0.3-2.2 \mathrm{GeV}\right)$ [3], VPI-GWU solutions FA02 $\left(\mathrm{T}_{\pi}=0-2.1 \mathrm{GeV}\right)$ and $\operatorname{SP} 06\left(\mathrm{~T}_{\pi}=0-2.5 \mathrm{GeV}\right)[5]$. In the column 2 and 3 those intervals of laboratory pion momentum and c.m.s. scattering angle are indicated, in which the existence of discrete ambiguities is mostly probable and, hence, measurements of the spin rotation parameters in $\pi p$ elastic scattering are needed first of all. Expected counting rates can be estimated using values of c.m.s. differential cross sections given in the column 4. A statistical precision at a level of $\Delta A(\Delta R) \approx 0.1$ is enough to distinguish different PWA solutions. The VPI-GWU experimental data volume is:

$$
\begin{array}{lll}
\text { SP06: } \mathrm{P}+=27190 / 13344 ; & \mathrm{P}-=22702 / 11967 ; & \mathrm{CX}=6084 / 2933 ; \\
\text { FA02: } \mathrm{P}+=21735 / 10468 ; & \mathrm{P}-=18932 / 9650 ; & \mathrm{CX}=4136 / 1690 ; \\
\text { SM95: } \mathrm{P}+=22616 / 10197 ; & \mathrm{P}-=18883 / 9421 ; & \mathrm{CX}=4402 / 1625 ;
\end{array}
$$

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Table 1: Elastic $\pi^{+} \mathrm{p}$-scattering
(Regions with presumed existence of discrete ambiguities)

| Number | Momentum region <br> $(\mathrm{MeV} / \mathrm{c})$ | Angle region <br> c.m.s.(deg.) <br> $700-900$ | Diff. cross section <br> $(\mathrm{mb} / \mathrm{sr})$ |
| :---: | :---: | :---: | :---: |
| 1 | $800-1000$ | $155-175$ | $0.03-0.18$ |
| 2 | $800-1200$ | $80-100$ | $0.08-0.60$ |
| 3 | $1600-1900$ | $50-70$ | $0.13-0.27$ |
| 4 | $1800-2100$ | $130-150$ | $0.08-0.30$ |
| 5 |  |  | $0.03-0.13$ |

Table 2: Elastic $\pi^{-} p$-scattering
(Regions with presumed existence of discrete ambiguities)

| Number | Momentum region <br> $(\mathrm{MeV} / \mathrm{c})$ | Angle region <br> c.m.s.(deg.) | Diff. cross section <br> $(\mathrm{mb} / \mathrm{sr})$ |
| :---: | :---: | :---: | :---: |
| 1 | $600-800$ | $60-80$ | $0.06-0.20$ |
| 2 | $600-800$ | $100-120$ | $1.0-1.4$ |
| 3 | $1200-1400$ | $150-170$ | $0.30-0.53$ |
| 4 | $1200-1500$ | $60-80$ | $0.05-0.23$ |
| 5 | $1200-1500$ | $90-110$ | $0.25-0.40$ |
| 6 | $1800-2100$ | $140-150$ | $0.002-0.010$ |
| 7 | $2000-2100$ | $130-150$ | $0.001-0.003$ |

## $\pi \mathrm{N}-\pi \mathrm{N}$ in J-PARC



Figure 1. Comparison of PWA's predictions
for $\pi^{+} p$ elastic scattering at $\mathrm{P}_{\pi}=700 \mathrm{MeV} / \mathrm{c}$.
$\pi \mathrm{N}-\pi \mathrm{N}$ in J-PARC


Figure 2. Comparison of PWA's predictions for $\pi^{+} p$ elastic scattering at $\mathrm{P}_{\pi}=793 \mathrm{MeV} / \mathrm{c}$.
$\pi \mathrm{N}-\pi \mathrm{N}$ in J-PARC


Figure 3. Comparison of PWA's predictions for $\pi^{+} p$ elastic scattering at $P_{\pi}=1700 \mathrm{MeV} / \mathrm{c}$.
$\pi \mathrm{N}-\pi \mathrm{N}$ in J-PARC


Figure 4. Comparison of PWA's predictions
for $\pi^{+} p$ elastic scattering at $P_{\pi}=1940 \mathrm{MeV} / \mathrm{c}$.
$\pi \mathrm{N}-\pi \mathrm{N}$ in J-PARC


Figure 5. Comparison of PWA's predictions for $\pi^{+} p$ elastic scattering at $P_{\pi}=1533 \mathrm{MeV} / \mathrm{c}$.
$\pi \mathrm{N}-\pi \mathrm{N}$ in J-PARC


Figure 6. Comparison of PWA's predictions for $\pi^{-}$p elastic scattering at $P_{\pi}=750 \mathrm{MeV} / \mathrm{c}$.


Figure 7. Comparison of PWA's predictions
$\pi \mathrm{N}-\pi \mathrm{N}$ in J-PARC


Figure 8. Comparison of PWA's predictions
for $\pi^{-} p$ elastic scattering at $P_{\pi}=1330 \mathrm{MeV} / \mathrm{c}$.
$\pi \mathrm{N}-\pi \mathrm{N}$ in J-PARC


Figure 9. Comparison of PWA's predictions
for $\pi^{-} p$ elastic scattering at $P_{\pi}=1450 \mathrm{MeV} / \mathrm{c}$.
$\pi \mathrm{N}-\pi \mathrm{N}$ in J-PARC


Figure 10. Comparison of PWA's predictions for $\pi^{-}$p elastic scattering at $\mathrm{P}_{\pi}=1850 \mathrm{MeV} / \mathrm{c}$.
$\pi N-\pi N$ in J-PARC


Figure 11. Comparison of PWA's predictions for $\pi^{-} p$ elastic scattering at $P_{\pi}=2070 \mathrm{MeV} / \mathrm{c}$.

## Experimental setup.

## 3. Experimental setup "SPIN-PMJ"

The spin rotation parameters A and R in $\pi \mathrm{N}$ elastic scattering are determined by the measurement of the polarization of recoiled protons produced by pions on a proton target polarized in the scattering plane. Polarization of the recoiled protons is measured through the asymmetry of their secondary scattering on the analyzing substance (carbon).

The apparatus is shown in Fig.12. Its basic elements are:
(i) Polarized proton target (PT);
(ii) Proton polarimeter included carbon filter (C), six sets of drift chambers (DC01-DC06) to detect the recoiled proton before and six sets of drift chambers (DC07-DC12) to detect the recoiled proton after pCscattering;
(iii) Six sets of drift chambers to detect the scattered pion (DC13-DC18);
(iv)Two pion beam multichannel hodoscopes G1 and G2;
(v) A number of scintillation counters (C1-C8) to provide the trigger and to identify the positive pions in the beam by the time of flight.


The experimental layout SPIN-PMJ (not to scale).
Figure 12. SPIN-PMJ setup. PT - polarized target; C1-C8 - scintillation counters;
G1, G2 - beam hodoscopes; DC01 - DC18 - drift chambers; C - carbon scatterer.


Polarized target section by horizontal plane.
Figure 13. 1 - window (stainless steel, 0.1 mm ); 2 - nitrogen screen (aluminum, 0.1 mm ); 3 - magnet; 4 - appendix with a container filled with the target material (aluminum alloy, 0.4 mm )

### 3.1. Polarized Target

The polarized proton target with arbitrary spin orientation in the horizontal plane has been built at PNPI especially for the measurements of the spin rotation parameters in the $\pi p$-elastic scattering (Fig.13.). A container filled with the target material (propanediole $\mathrm{C}_{3} \mathrm{H}_{8} \mathrm{O}_{2}$ doped by $\mathrm{Cr}^{V}$ complexes) is placed into magnetic field of 2.5 T created by a Helmholtz pair of superconductive coils [11].

The container has a cylindrical form with vertical size and diameter of $30 \mathrm{~mm} \times 30 \mathrm{~mm}$. Cooling of the target down to 0.5 K is provided by an evaporation-type ${ }^{3} \mathrm{He}$-cryostat.The polarization is pumped by the dynamic nuclear orientation method up to the absolute value of $70-80 \%$ with an uncertainty of $1.5 \%$. The method of proton magnetic resonance (PMR) is used for the polarization measurements. These measurements are based on the calculations of area under the PMR curve. The equipment is calibrated on the equilibrium target polarization at temperature of 0.5 K .

$\pi \mathrm{N}-\pi \mathrm{N}$ in J-PARC

### 3.2.Proton polarimeter

Recoil proton polarimeter consists of two sets of one-coordinate drift chambers (six chambers in each set) and carbon block. The accuracy of determinations of the secondary scattering angle is near $1^{0}$.

The average analyzing power for selected events is usually between $0.1-0.3$. For realization of presented proposal it is necessary to have possibility to measure the normal components of recoil proton polarization in the proton energy range from 100 to 1600 MeV and to know the pC -analyzing power in this energy region. The PNPI-ITEP collaboration performed the associated investigations. At the first step the existing till now world experimental data were collected and pC -analyzing power has been investigated as a function of proton scattering angle $\theta_{\mathrm{pC}}$, proton kinetic energy $\mathrm{T}_{\mathrm{P}}$ and energy losses in the process pC scattering $\mathrm{E}^{\prime}$ in this energy range [12]. At the next step the pC analyzing power for polarized protons has been experimentally measured by PNPI-ITEP collaboration for proton beam momentum of $1.36,1.60,1.78$ and $2.02 \mathrm{GeV} / \mathrm{c}$ and for carbon scatterer thickness of $4.9,19.4$ and $36.5 \mathrm{~g} / \mathrm{cm}^{2}$. These data have been compared with previous results [12] and used to fit analyzing power obtained for various proton energies and scattering angles [13]. For the spin rotation parameters A and R measurements the thickness of carbon blocks will be optimized in accordance with recoil proton energy and range [12].

The carbon (graphite GMZ) is $99.9 \%$ pure.

## 5.Experimental setup "SPIN-PMJ" arrangement at J-PARC pion beam.

The distance between polarized target and last magnet element of the pion channel should be more than 3 m for the beam pion direction determinations.
The height of the polarized target container over the experimental hall floor should be more than 1.3 m . This is defined by PT constructions.
The full size of the experimental setup is 6 m perpendicularly to the pion beam $(3 \mathrm{~m}+3 \mathrm{~m})$ and 8 m along the pion beam.
It is necessary that the full height of the experimental hall must be more than 3.5 m in the SPIN-PMJ setup region for the polarized target service.

## $\pi \mathrm{N}-\pi \mathrm{N}$ in J-PARC

## 4.Conclusion

The experimental program includes the measurement of the spin rotation parameters $A$ and $R$ at 7-8 meanings of the pion beam momentum, where the existence of discrete ambiguities is mostly probable. These data will be used in performing the new PWA for obtaining the unambiguous behavior of a zero trajectory at "critical points" [6] and to exclude the twofold ambiguities from the $\pi \mathrm{N}$-amplitudes.

After this procedure, some additional measurements can be necessary for a completion of the elastic channel investigation in the baryon resonance region.
In the following, the main elements of SPIN-PMJ experimental set can be used for the investigation of the polarization parameters in the other channels of the pion-nucleon interactions in the resonance region $[1,16]$.

Today the collaboration has the polarized target and scintillation counters. The drift chambers are being designed. The cost of the first two DC production is near 7200 Euro, every next two DC cost is estimated as 5400 Euro. The price of all 18 DC for SPIN-PMJ is estimated near 50400 Euro. The cost of two hodoscopes production is estimated near 9400 Euro.
$\pi \mathrm{N}-\pi \mathrm{N}$ in J-PARC
Table 1: Parameters of the $\mathrm{N}^{*}$ - resonances.

| $\begin{aligned} & \text { PDG } \\ & (2002) \end{aligned}$ | $\mathbf{L}_{\mathbf{I}, \mathbf{2 J}}$ | Status | $\begin{gathered} \text { KA84 } \\ (1984) \end{gathered}$ | $\left({ }^{3} \mathbf{P}_{0}\right) \text { model }$ <br> (1994) | $\begin{aligned} & \text { SM95 } \\ & (1995) \end{aligned}$ | $\begin{aligned} & \text { FA02 } \\ & (2003) \end{aligned}$ | Skyrme (1985) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| N(1440) | $\mathbf{P}_{11}$ | **** | 1410(135) | 1540 | 1467(440) | 1468(360) | ---- |
| N(1520) | $\mathrm{D}_{13}$ | **** | 1519(114) | 1495 | 1515(106) | 1516(98) | 1715 |
| N(1535) | $S_{11}$ | **** | 1526(120) | 1460 | 1535(66) | 1547(178) | 1478 |
| N(1650) | $S_{11}$ | **** | 1670(180) | 1535 | 1667(90) | 1651(130) | ---- |
| ---- | $S_{11}$ | ---- | ---- | ---- | 1712(174) | ---- | ---- |
| N(1675) | $\mathbf{D}_{15}$ | **** | 1679(120) | 1630 | 1673(154) | 1676(152) | 1744 |
| N(1680) | $\mathbf{F}_{15}$ | **** | 1684(128) | 1770 | 1678(126) | 1683(134) | 1823 |
| N(1700) | $\mathbf{D}_{13}$ | *** | 1731(110) | 1625 | ---- | ---- | ---- |
| N(1710) | $\mathbf{P}_{11}$ | *** | 1723(120) | 1770 | [1770-i189] | ---- | 1427 |
| N(1720) | $\mathbf{P}_{13}$ | **** | 1710(190) | 1795 | 1820(354) | 1750(256) | 1982 |
| N(1900) | $\mathbf{P}_{13}$ | ** | ---- | 1870 | ---- | ---- | ---- |
| ---- | $\mathbf{P}_{11}$ | ---- | ---- | 1880 | ---- | ---- | ---- |
| ---- | $\mathbf{P}_{13}$ | ---- | ---- | 1910 | ---- | ---- | ---- |
| ---- | $\mathbf{P}_{13}$ | ---- | ---- | 1950 | ---- | ---- | ---- |
| ---- | $\mathbf{P}_{11}$ | ---- | ---- | 1975 | ---- | ---- | ---- |
| ---- | $F_{15}$ | ---- | ---- | 1980 | ---- | ---- | ---- |
| N(1990) | $\mathbf{F}_{17}$ | ** | 2005(350) | 1980 | ---- | ---- | 2011 |
| N(2000) | $F_{15}$ | ** | 1882(95) | 1995 | 1814(176) | ---- | ---- |
| ---- | $\mathbf{P}_{13}$ | ---- | ---- | 2030 | ---- | ---- | ---- |
| ---- | $\mathbf{S}_{11}$ | ---- | ---- | 2030 | ---- | ---- | ---- |
| ---- | $\mathrm{D}_{13}$ | ---- | ---- | 2055 | ---- | ---- | ---- |

## $\pi \mathrm{N}-\pi \mathrm{N}$ in J-PARC

Table 2. Parameters of the $\Delta$ - resonances.

| PDG | $\mathbf{L}_{3,2 \mathrm{~J}}$ | Status | KA84 | $\left({ }^{3} \mathrm{P}_{0}\right)$ model | SM95 | FA02 | Skyrme |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (2002) |  |  | (1984) | (1994) | (1995) | (2003) | (1985) |  |
| $\Delta(1232)$ | $\mathbf{P}_{33}$ | **** | 1233(116) | 1230 | 1233(114) | 1233(118) | 1424 |  |
| $\Delta(1600)$ | $\mathrm{P}_{33}$ | *** | 1522(222) | 1795 | [1675-i193] | ---- | 1435 |  |
| $\Delta(1620)$ | $\mathrm{S}_{31}$ | **** | 1610(139) | 1555 | 1617(108) | 1614(141) | 1478 |  |
| $\Delta(1700)$ | $\mathrm{D}_{33}$ | **** | 1680(230) | 1620 | 1680(272) | 1688(365) | 1737 |  |
| $\Delta(1750)$ | $\mathbf{P}_{31}$ | * | ----- | 1835 | ---- | ----- | ---- |  |
| $\Delta(1750)$ | $\stackrel{F}{5}^{35}$ | ---** |  | 1910 | ---- | ---- | ---- |  |
| $\Delta(1900)$ | $\mathrm{S}_{31}^{35}$ | *** | 1908(140) | 2035 | ---- | ---- | ---- |  |
| $\Delta(1905)$ | $\mathrm{F}_{35}$ | **** | 1905(260) | ---- | 1850(294) | 1856(334) | 1931 |  |
| $\Delta(1910)$ | $\mathrm{P}_{31}$ | **** | 1888(280) | 1875 | 2152(760) | 2333(1128) | 1982 |  |
| $\Delta(1920)$ | $\mathrm{P}_{33}$ | *** | 1868(220) | 1915 | ---- | ----- | 1946 |  |
| $\Delta(1930)$ | $\mathrm{D}_{35}$ | *** | 1901(195) | 2155 | 2056(590) | 2046(402) | 1730 |  |
| $\Delta(1940)$ | $\mathrm{D}_{33}$ | * | --- | 2080 | --- | --= |  |  |
| $\Delta(1950)$ | $\mathrm{F}_{37}$ | **** | 1923(224) | 1940 | 1921(232) | 1923(278) | 1816 |  |
|  | $\mathbf{P}_{33}$ | ---- | -=-- | 1985 | ---- | ---- | --- |  |
| $\Delta(2000)$ | $\mathrm{F}_{35}$ | ** | ---- | 1990 | ---- | ---- | ---- |  |
|  | $\mathrm{D}_{33}$ | ---- | ---- | 2145 | ---- | ---- | ---- |  |
| $\Delta(2150)$ | $\stackrel{\mathbf{S}_{31}}{ }$ | * |  | 2165 2140 | ----- | ----- |  |  |
| $\Delta(2200)$ | $\mathrm{G}_{37}$ | * | 2215(400) | 2230 | ---- | ---- | 2162 |  |
| --- | $\mathrm{G}_{37}$ | ---- | ----- | 2295 | ---- | ---- | ---- |  |
| $\Delta(2300)$ | ${ }_{\sim}^{\mathbf{D}_{35}}$ | ** | 2217(300) | 2325 2420 | ----- | ----- | 2407 |  |
| $\Delta(2350)$ | $\mathrm{D}_{35}$ | * | 2305(300) | 2265 | ---- | ---- | ---- |  |
| $\Delta(2390)$ | $\mathrm{F}_{37}$ | * | 2425(300) | 2370 | ---- | ---- | 2083 |  |
| $\Delta(2400)$ | $\mathrm{G}_{39}$ | ** | 2468(480) | 2295 | ---- | ---- | ---- |  |
| $\Delta(2420)$ | $\mathrm{H}_{3,11}$ | **** | 2416(340) | 2450 | ---- | ---- | 2327 |  |
| --- | $\mathbf{F}_{3}{ }^{37}$ | ---- | ----- | 2460 | ---- | ---- | ---- |  |
|  | $\mathrm{H}_{39}$ |  |  | 2505 |  |  |  |  |
| $\Sigma$ |  | I 16 |  | I 27 | I 8 | I 7 | I 13 | I |

$\pi \mathrm{N}-\pi \mathrm{N}$ in J-PARC
50GeV MR Main Parameters

| Parameters | 1567.5 m |
| :--- | :--- | :--- |
| Circumference | 249.475 m |
| Average Radius |  |
| Injection Energy |  |
| Extraction Energy | 3 GeV |
| Particle Per Pulse | 50 GeV |
| Revolution Period | $3.3 \times 10^{14}$ |
| at Injection | $5.384 \mu \mathrm{~s}$ |
| at Extraction | $5.230 \mu \mathrm{~s}$ |
| Repetition Rate |  |
| Ramping Pattern | 0.3 Hz |
| Injection | 0.17 s |
| Acceleration | 1.96 s |
| parabola+Linear+Parabola | 0.13 s |
| linear | 1.7 s |
| parabola | 0.13 s |

Construction Schedule


## Drift chambers



Drift chambers


## Polarized target

## Polarized proton target

## 1. General description.

Polarized proton target with vertical spin orientation of polarized protons is used. More detailed description is given in the paper[1]. The target construction provides the possibility to rotate its cryostat around vertical axis. This allows to increase the window for outlet particles so that the setup possibilities can be improved substantially (fig. 1). Fig. 1 presents the view from above (in the plane of $\pi \mathrm{N}$-elastic scattering). The section in the horizontal plane and possible scattering angles are shown.
E.I. Bunyatova et al. Preprint PNPI-1191, 1986, 18 p.

Polarized target.


Fig. 1. Target: top view plane. There are shown:
$\mathbf{1}$ - target window, $\mathbf{2}$ - nitrogen screen,
3 - magnet area, 4 - container with the target properly.

Fig. 2.
Target in the vertical sectional view.


1 - helium-3 pump-out
2 - neck
3 - helium-4 pump-out
4,11 - nitrogen screens
5,21 - helium inputs
6- nitrogen tank
7 - magnet
8 - window
9 - magnet frame
10 - housing
12 - indium compaction
13 - rotating tee-joint
14 - helium-4 output through currentinput
15 - connection to current source
16 - current-input compaction and
helium-4 output
17 - current-input
18 - helium tank (at 4.2 K )
19 - refrigerator
20 - appendix with $\operatorname{target}\left(\mathrm{C}_{3} \mathrm{H}_{8} \mathrm{O}_{2}\right)$ matter

## Electronic providing of the polarized target.

*the area under the PMR curve is determined using a Q meter
*the measuring circuit of which is excited by a high-frequency fixed-amplitude current
*Remote computer PC1 contains a crate controller board and exercises direct control over the measuring system through the CAMAC crate
*An RF generator controlled by the sweep DAC produces a saw-tooth sweep
*ADC measures the voltage across the $Q$ meter in each scanning cycle
*This system also comprises four adjustment DAC: tuning reference voltage phase, to adjust the measuring circuit, to select the PMR frequency (the RF generator frequency) and to control the magnetic field


## The experiment planning by the zero trajectory consideration.

## $\partial$

\{ Barrelet method employment. \}
The basic idea of the Barrelet methods is to represent the transverse amplitudes F§ at fixed energy by the flilding ansatz, which exhibits the zeros in the complex $z=\cos \theta_{\mathrm{cm}}$ - plane:

$$
\mathbf{I}_{\mathrm{F}(\cong ; \mathrm{z})=\mathrm{F}(1) \times{ }_{\mathrm{i}=1}^{\mathrm{N}}\left[\left(\mathrm{z}-\mathrm{z} \cong_{\mathrm{i}}\right) /\left(1-\mathrm{z} \cong_{\mathrm{i}}\right)\right] \times \mathrm{R}(\cong ; \mathrm{z}) ; \mathrm{R}(\cong ; 1)=1 . . . . . . .}
$$

as functions of a variable $\omega$, which is connected with z by a conformal mapping $\mathrm{e}^{\mathrm{i} \theta}=\mathrm{z} \cong\left(\mathrm{z}^{2}-1\right)^{1 / 2}$. When $\theta$ is real, it corresponds to the center-of-mass scattering angle. This mapping has the property, that a physical value of $z$ (i.e. $z$ real and $|z|<1$ ) is mapped onto two points in the $\omega$-plane, which lies on the upper and lowr halves of the unit circle, respectively. Here $\omega$ and $\omega^{-1}$ belong to the same value of $z$..

Transverse amplitudes have the advantage, that their modulus can be determined from $\mathrm{d} \sigma / \mathrm{d} \Omega$ and P alone $\mid F \cong=d \sigma / d \Omega \times(1 \cong P)$.
This equation shows that the zeros of the amplitude can be derived from the zeros of do/d $\Omega$ and P data but, unfortunately, there is a $2{ }^{2 N}$ fold ambiguity because for each pair of zeros $z_{i}$ and $z_{i}^{*}$ (or $\omega_{i}$ and $1 / \omega_{i}^{*}$ ) one ha the choice whether $\mathrm{z}_{\mathrm{i}}$ or $\mathrm{z}_{\mathrm{i}}$ * belongs to the amplitude F .
The spin rotation parameters A and R measurements can help in such choice.
Qhe positions of the zeros of $\mathrm{F} \cong$ depends of course on the incident pion beam momentum.
This allows one to locate problems of the unknown PWA ambiguities simply by looking at the zero
tragctories on the $\omega$ - planes which are near the physical region.
 X
$\rho$
$\rho$

TT

Zero trajectories and experiment planning.

## $\rho$



## $\rho$



## Zero trajectories FA02.



## Zero trajectories CMB.



