

# *A Microscopic Approach to Hyperon-Nucleon and Hyperon-Hyperon Interactions in Hypernuclei*

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## 1. Introduction

## 2. A strategy --- theoretical ---

## 3. Examples

3.1.  $\Lambda^3\text{H}$  Faddeev calculation

3.2. Spin-orbit splitting of  $\Lambda^9\text{Be}$

3.3. Nagara event:  $\Lambda\Lambda^6\text{He}$

## 4. Summary

# J-PARC: many experimental data

*B<sub>8</sub>B<sub>8</sub> interactions*

*NN, YN, YY ... interactions*

spin-flavor  $SU_6$  symmetry  
flavor  $SU_3$  symm. breaking  
 $\pi$ -on effect ... chiral symm.

finite nuclei

nuclear matter  
neutron stars

hypernuclei

strange matter

phase shifts

G-matrix

effective interaction

YN, YY interactions are relatively weak !

## *Different approaches to different categories*

- ***s*-shell hypernuclei:**  ${}_{\Lambda}^3\text{H}$ ,  ${}_{\Lambda}^4\text{H}$ ,  ${}_{\Lambda}^4\text{He}$ ,  ${}_{\Lambda}^5\text{He}$  ...  
**rigorous few-body calculations, using the bare interactions, are possible**
- ***p*-shell hypernuclei:**  ${}_{\Lambda}^9\text{Be}$ ,  ${}_{\Lambda}^6\text{Li}$ ,  ${}_{\Lambda}^{12}\text{C}$ ,  $({}_{\Lambda\Lambda}^6\text{He})$ ,  
 ${}_{\Lambda\Lambda}^{10}\text{Be}$  ...  **$\alpha$ -cluster models are efficient**
- **medium and heavy hypernuclei:**  ${}_{\Lambda}^{89}\text{Y}$  ...  
**mean field approach based on *G*-matrix + Thomas Fermi approximation**
- **strange matter and high density matter**  
***G*-matrix and variational**

**A small number of experimental data are essential :  
for example,**

- $B_{\Lambda}(\Lambda^3\text{H}) = 130 \pm 50 \text{ keV}$ : **triton binding energy**
- $B_{\Lambda}(\Lambda^5\text{He}) = 3.12 \pm 0.02 \text{ MeV}$ : **overbinding problem**
- $\Delta B_{\ell s}(3/2^+ - 5/2^+) = 43 \pm 5 \text{ keV}$  :  **$\ell s$  splitting of  $\Lambda^9\text{Be}^*$**
- $\Delta B_{\Lambda\Lambda} = 1.01 \pm 0.20 \text{ MeV}$  : **Nagara event**
- . . . .

**To make the most of these experimental data,  
the OCM (orthogonality condition model) and  
simple boson models are not sufficient ...**

**3-cluster Faddeev formalism  
using 2-cluster RGM kernels**

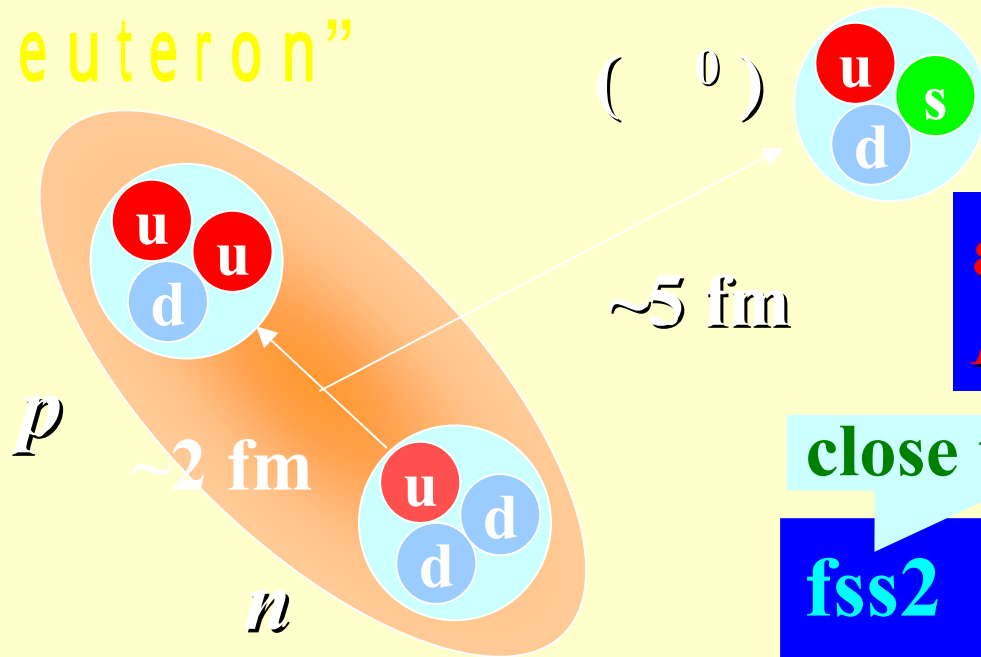
# $^3_{\Lambda}\text{H}$ (hypertriton)

PRC 70, No. 2 (2004)

$\Lambda N$  on-shell properties are directly reflected

$^1S_0 / ^3S_1$  relative strength

“deuteron”



exp't

$$\varepsilon_d = 2.22 \text{ MeV}$$

$$B = 130 \pm 50 \text{ keV}$$

close to NSC89  $P_{\Sigma}$  (%)

fss2 289 keV 0.80

FSS 878 keV 1.36

150 channel calculation

$$\varepsilon_{NN} = 19.37 - 21.03 = -1.66$$

$$|\varepsilon_d| = 17.50 - 19.72 = -2.22$$

(MeV)

## $\Lambda N$ $^1S_0$ and $^3S_1$ effective range parameters

model	$a_s$ (fm)	$r_s$ (fm)	$a_s$ (fm)	$r_t$ (fm)	$B_\Lambda$ (keV)	$P_\Sigma$ (%)
<b>FSS</b>	<b>- 5.41</b>	<b>2.26</b>	<b>- 1.03</b>	<b>4.20</b>	<b>878</b>	<b>1.36</b>
<b>fss2</b>	<b>- 2.59</b>	<b>2.83</b>	<b>- 1.60</b>	<b>3.01</b>	<b>289</b>	<b>0.80</b>
<b>NSC89</b>	<b>- 2.59</b>	<b>2.90</b>	<b>- 1.38</b>	<b>3.17</b>	<b>143</b>	<b>0.5</b>
<b>“fss2”</b>	<b>- 2.15</b>	<b>3.05</b>	<b>- 1.80</b>	<b>2.87</b>	<b>145</b>	<b>0.53</b>

“fss2”:  $m_\kappa c^2 = 936$  MeV  $\rightarrow$  1,000 MeV

favorable for  ${}_\Lambda^4\text{H} (1^+)$  ?

$B_\Lambda$ (keV)	fss2	“fss2”
6 ch ( $S$ )	137	44
15 ch ( $SD$ )	198	85
102 ch ( $J \leq 4$ )	288	145
150 ch ( $J \leq 6$ )	289	145

*Effect of the higher partial waves*

$B^{\text{exp}} = 130 \pm 50$  keV

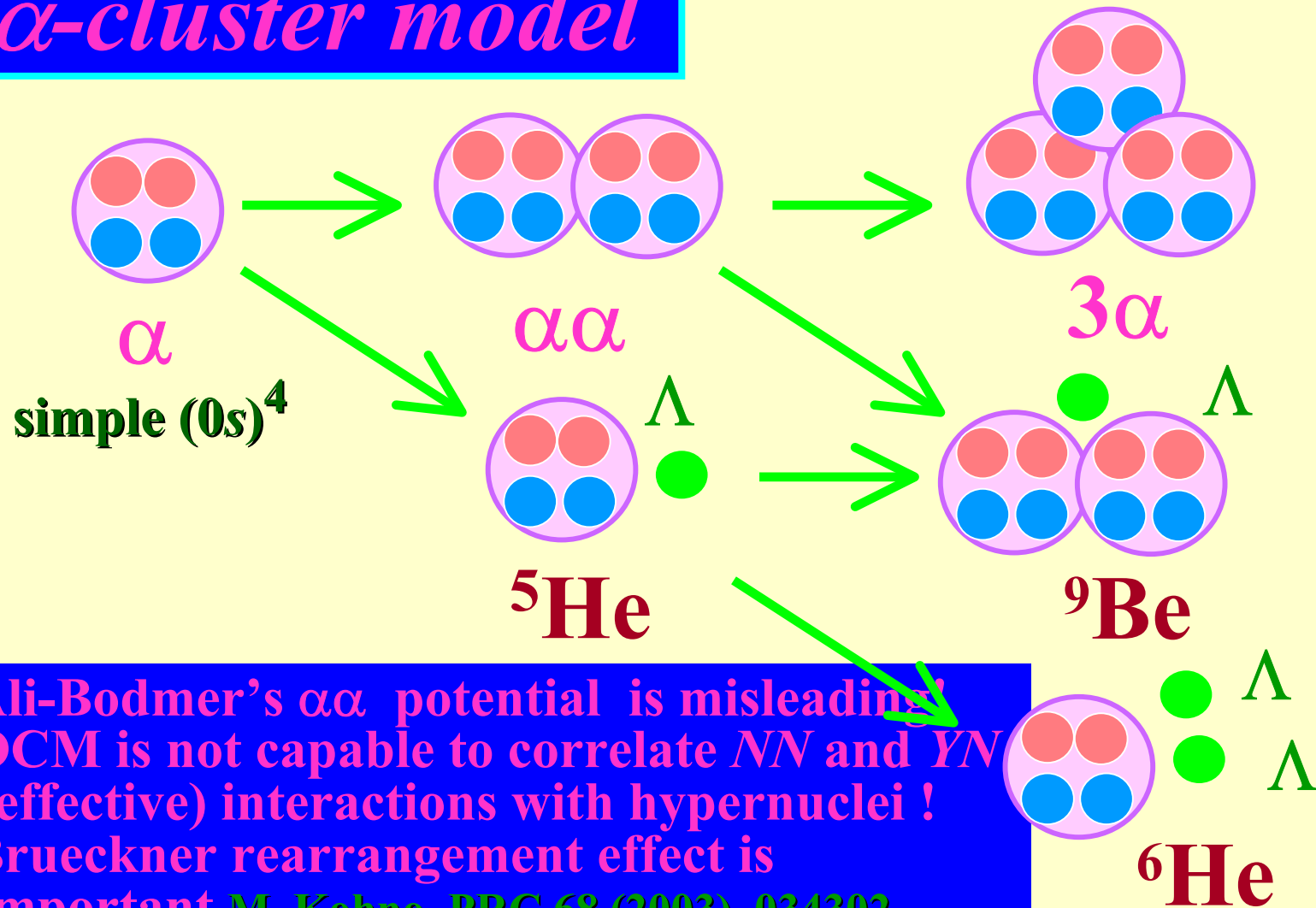
$V_{\Lambda N}$	$a_s$ (fm)	$a_t$ (fm)	$B_{\Lambda}$ (keV)
NSC89	- 2.59	- 1.38	143
NSC97f	- 2.51	- 1.73	80
NSC97e	- 2.10	- 1.83	23
NSC89(S)	- 3.39	- 1.38	$0.37 \cdot 10^3$
NSC97f(S)	- 2.82	- 1.72	$0.18 \cdot 10^3$
NSC97e(S)	- 2.37	- 1.83	$0.10 \cdot 10^3$
exp't			$130 \pm 50$

upper: Faddeev by A. Nogga et al. Phys. Rev. Lett. 88, 172501 (2002)

lower: variaton by H. Nemura et al. Phys. Rev. Lett. 89, 142504 (2002)

**Simulated potentials in *s*-shell  $\Lambda$ -hypernuclei are misleading!**

# *$\alpha$ -cluster model*



- Ali-Bodmer's  $\alpha\alpha$  potential is misleading!
- OCM is not capable to correlate  $NN$  and  $YN$  (effective) interactions with hypernuclei !
- Brueckner rearrangement effect is important M. Kohno PRC 68 (2003) 034302



# 3 $\alpha$ Faddeev for $^{12}\text{C}(0_1^+)$

Cut-off Coulomb with  $R_C=10$  fm in Faddeev

Ali-Bodmer

Fad.

-1.53

RGM Fad.

Fukushima  
Kamimura  
(1977)

-5.97

-7.5

GCM Fad.

Uegaki  
(1977)

-5.37

-6.9

SVM Fad.

Suzuki  
(2002)

Exp: -7.3 MeV

*3 cluster exchange effect is small!*

-9.59

effective NN force

VN2

-0.245

VN1

0.18

MN(3R)

0.14 MeV for  $E_{2\alpha}(0^+)$

Fujiwara, Miyagawa, Kohno, Suzuki, Baye, Sparenberg, PRC 70, No. 2 (2004)

(3.04 MeV) 2+

# 2 $\alpha\Lambda$ Faddeev for ${}^9_{\Lambda}\text{Be}$

PRC 70, No. 2 (2004)

(0) 92 keV 0+

$\alpha + \alpha + \Lambda$

${}^8\text{Be}$

( $u = 0$  SB)

exp't

MN+SB forces

-3.12 $\pm$ 0.02 MeV

$\alpha + {}_{\Lambda}{}^5\text{He}$

(3067 $\pm$ 3 $\pm$ 1 keV)

3/2<sup>+</sup>

(2.92 MeV)

(3024 $\pm$ 3 $\pm$ 1 keV)

5/2<sup>+</sup>

Ali-Bodmer's  $\alpha\alpha$  potential leads to overbinding !

-6.62 $\pm$ 0.04 MeV

1/2<sup>+</sup>

-6.84 MeV

${}_{\Lambda}{}^9\text{Be}$

calc.

$\Delta E(3/2^+ - 5/2^+) = 43 \pm 5$  keV

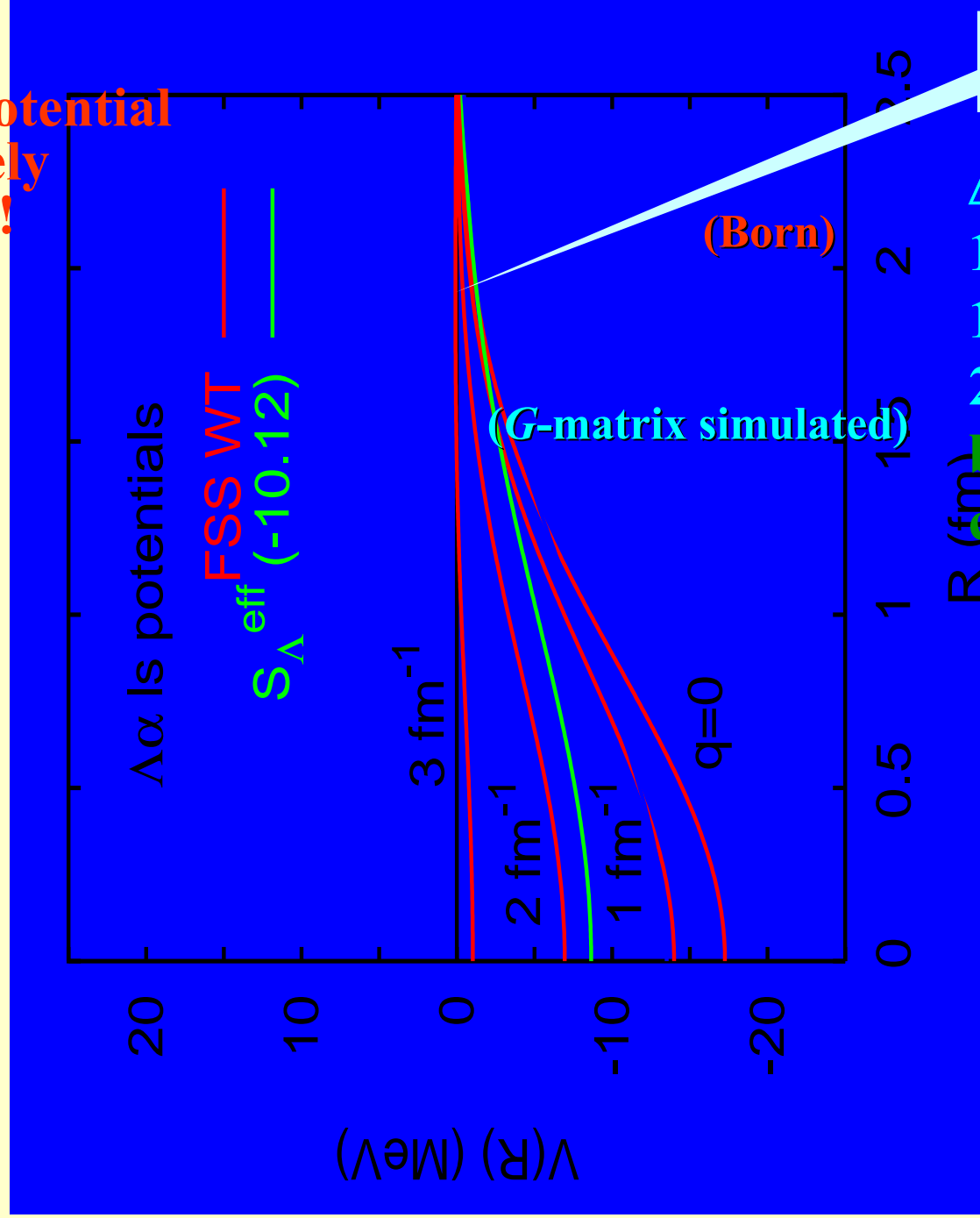
Akikawa et al.  
PRL 88 (2002) 082501

198 keV (fss2 quark (86 keV) + EMEP)  $\rightarrow$   $\sim$ 40 keV

137 keV (FSS) by Born kernel  
( $u = 0.82$  SB)

in short-range correlations ?

Folding potential  
is extremely  
non-local !



$$S_{\Lambda}^{\text{eff}} = \left(1 + \frac{M_{\Lambda}}{4M_N}\right) \times S_{\Lambda}$$

$\Delta E_{\ell s} =$   
137 keV  
147 keV  
209 keV

by Faddeev  
calculations

*Scheerbaum factors  $S_\Lambda$  in symmetric nuclear matter ( $k_F=1.07 \text{ fm}^{-1}$ ) by G-matrix calculations*

$^1P_1 - ^3P_1$

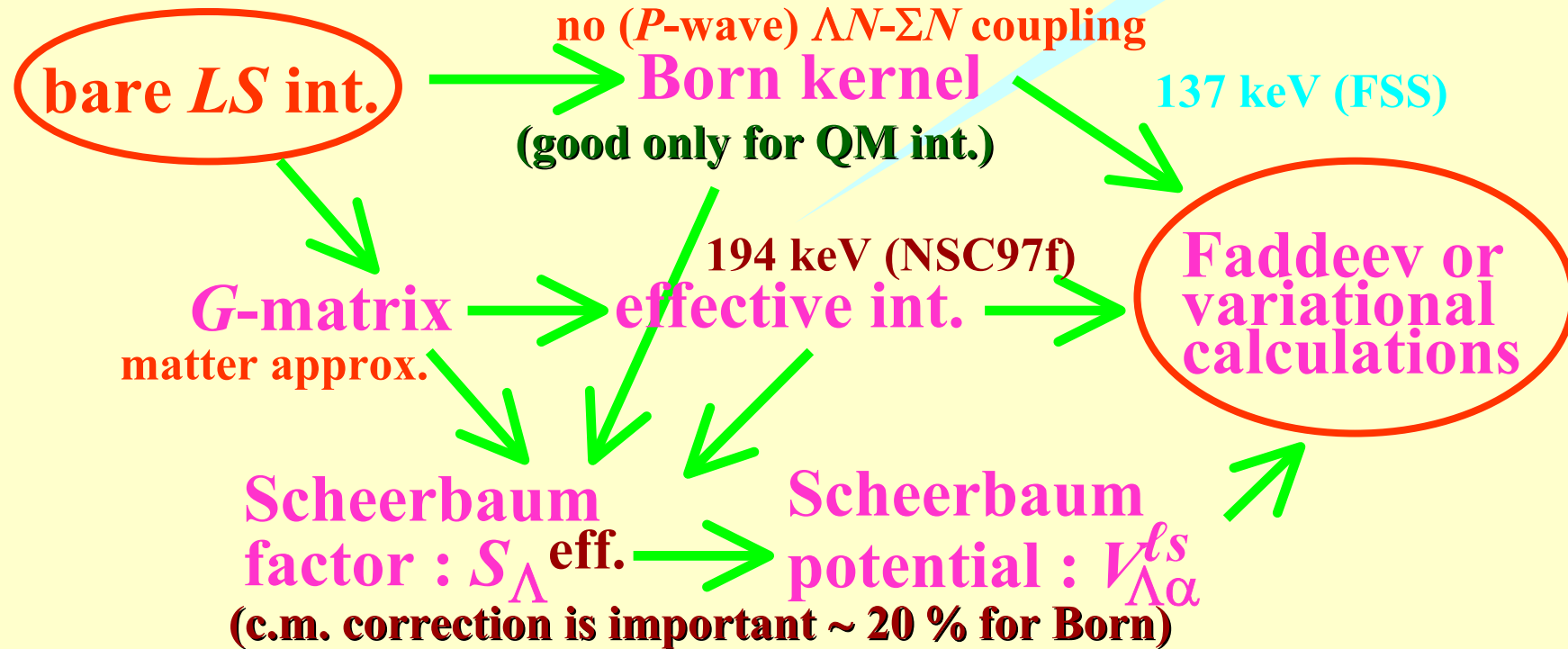
model		full		<i>P-wave</i> $\Lambda N$ - $\Sigma N$ coupling off	
		odd	even	odd	even
FSS	<i>LS</i>	- 17.36	0.38	- 19.70	0.30
	<i>LS</i> (-)	24.83	0.22	8.37	0.26
	total	<b>- 1.93</b>		<b>- 10.77</b>	
fss2	<i>LS</i>	- 19.97	- 0.14	- 21.04	- 0.20
	<i>LS</i> (-)	8.64	0.21	6.12	0.23
	total	<b>- 11.26</b>		<b>- 14.89</b>	

**EMEP *LS* force is unfavorable !**

**Unit: MeV·fm<sup>5</sup>**

# Comparison of different methods

0.16 MeV  
by Hiyama



**Results are different in all the cases !  
Comparison in the same condition is necessary.**

# 2 $\Lambda\alpha$ Faddeev for ${}_{\Lambda\Lambda}{}^6\text{He}$ using $\Lambda\Lambda$ RGM T-matrices of fss2 and FSS

$$B_{\Lambda\Lambda} = B_{\Lambda\Lambda}({}_{\Lambda\Lambda}{}^6\text{He}) - 2B_{\Lambda}({}_{\Lambda}{}^5\text{He}) = 1.01 \pm 0.20 \text{ MeV}$$

H. Takahashi et al. PRL 87 (2001) 21250

1.14  
in SC

$V_{\Lambda N}$	$V_{\Lambda\Lambda}(3G)$	FSS	fss2	SB (2G)
SB	3.62	3.65	<b>1.41</b>	1.90

## Effects not considered

PRC 70, No. 3 (2004)

1. ( $\alpha\Lambda\Lambda$ )-( $\alpha\Xi N$ )-( $\alpha\Sigma\Sigma$ ) CC effect (fss2, FSS)  $\sim 0.5 \text{ MeV} ?$
2. Brueckner rearrangement effect of  $\alpha$ -cluster (starting energy dependence of the  $\Lambda N$  interaction)  $\sim -1 \text{ MeV}$

M. Kohno PRC 68 (2003) 034302

3. quark Pauli effect by Suzuki and Nemura  $< -0.2 \text{ MeV}$

PTP 102 (1999) 203

**fss2 is consistent with the Nagara event !**

# Summary

We should use most appropriate approaches to the systems considered. For the  $s$ -shell hypernuclei, **the bare interactions should be used without alteration**. For  $p$ -shell hypernuclei, advantages and disadvantages of various approaches should be critically examined. The linkage between the effective interactions and the bare interactions is usually very difficult. However, the **3-cluster Faddeev formalism using 2-cluster RGM kernels** provides a useful framework, not only for using the quark-model baryon-baryon interactions in the study of few-baryon systems, but also for studying cluster structure of light hypernuclei. **Characteristic features of this formalism are 1) the input is closer to the bare  $YN$  and  $YY$  interactions and 2) the Faddeev results exactly coincide with the variational calculations as long as the full model space is used.**